$$\operatorname{cov}\left(\theta_t, \theta_s\right) = \begin{cases} \tilde{\theta} & \forall\ t = s \\ 0 & \text{otherwise} \end{cases}$$